

Title: Hausdorff measure for continued fraction iterated function system.

Abstract: Let G be the infinite iterated function system corresponding to the Gauss map, i.e. G is the collection of maps $g_k(x) = \frac{1}{x+k}$, $k \in \mathbb{N}$.

Next, let G_n be the finite subsystem built by restricting the collection of maps g_k to n initial ones.

Let $J_n(G)$ be the limit set of the subsystem G_n . This is the set of irrational numbers whose infinite continued fraction expansions have all entries in the finite set $\{1, 2, \dots, n\}$. Denote by $h_n < 1$ its Hausdorff dimension. In my previous work joint with Mariusz Urbański we proved the following continuity result: let H_n be the Hausdorff measure of $J_n(G)$, evaluated at its Hausdorff dimension h_n . Then $\lim_{n \rightarrow \infty} H_n = 1$. The main difficulty comes from the fact that the numerical value of Hausdorff measure is not directly visible by tools of thermodynamic formalism.

In this talk, I will present a new result showing exact asymptotics of H_n . This asymptotic behaviour is different from that for h_n . The talk is based on joint work with Rafał Tryniecki and Mariusz Urbański.