



# Highlights from the Saclay workshop “Ultimate precision at hadron colliders”

**Alessandro Vicini**  
University of Milano, INFN Milano

Pisa, February 7th 2020

# Schedule of the workshop

first week: PDF

EW precision measurements

low-energy observables

second week: Higgs and high-energy probes  
global interpretation

WEDNESDAY, 27 NOVEMBER

09:00 → 11:00 **Measurements of EW precision observables**  
Conveners: Alessandro Vicini (Università degli Studi e INFN Milano (IT)), Mika Anton Vesterinen (University of Warwick (GB)), Ulla Blumenschein (University of London (GB))

10:00 **Measurement of  $m_W$  : experimental and theoretical requirements**

Speaker: Stefano Camarda (CERN)

wmass.pdf

11:00 → 11:30 **Break**

11:30 → 12:30 **Measurements of EW precision observables**

Conveners: Alessandro Vicini (Università degli Studi e INFN Milano (IT)), Mika Anton Vesterinen (University of Warwick (GB)), Ulla Blumenschein (University of London (GB))

11:30 **Measurement of  $\sin^2 \theta$  : experimental and theoretical requirements**

Speaker: Arie Bodek (University of Rochester (US))

Mixing\_angle-Bode...

12:30 → 14:00 **Lunch**

14:00 → 18:00 **Informal discussions: 2**

THURSDAY, 28 NOVEMBER

09:00 → 12:30 **Measurements of EW precision observables: QCD issues in the high-precision determination of EW parameters**

Conveners: Alessandro Vicini (Università degli Studi e INFN Milano (IT)), Mika Anton Vesterinen (University of Warwick (GB)), Ulla Blumenschein (University of London (GB))

09:15 **Experimental challenges: high- vs low-pileup measurements**

Speaker: Josh Bendavid (CERN)

expChallengesEWK...

09:50 **Revisiting the estimate of PDF uncertainties**

Speaker: Emanuele Angelo Bagnaschi (Paul Scherrer Institut)

OrsayWorkshop-Ba...

10:25 **Coffee Break**

11:05 **Ultimate QCD tools**

Speaker: Thomas Gehrmann

Ultimate\_Gehrman...

11:40 **Discussion**

14:00 → 17:30 **Measurements of EW precision observables: Towards a global EW fit**

Conveners: Alessandro Vicini (Università degli Studi e INFN Milano (IT)), Mika Anton Vesterinen (University of Warwick (GB)), Ulla Blumenschein (University of London (GB))

14:00 **Combination of MW / sin<sup>2</sup>theta final values obtained at different colliders/experiments**

Speaker: Nansi Andari (Université Paris-Saclay (FR))

presentation\_andar...

14:35 **Global EW fits: experimental and theoretical issues**

Speaker: Matthias Schott (CERN / University of Mainz)

LHC\_Ultimate\_Prec...

15:10 **Discussion**

15:30 **Coffee break**

16:00 **O(alpha<sup>2</sup>) initial state QED corrections in e+e- -> f bbar**

Speaker: Kay Schönwald (DESY)

talk-schoenwald.pdf

16:35 **Towards fully NLO-EW analyses**

Speaker: Mauro Chiesa (University of Würzburg)

chiesa\_orsay.pdf

17:10 **Discussion**

# Different open problems and challenges

## Theory

role of higher-order corrections in the description of differential observables (Gehrmann)

impact of the QCDxEW interplay in the MW determination (Chiesa)

role the input scheme in the  $\sin^2\theta_{\text{eff}}$  determination (Chiesa)

relevance of the PDF correlations in the MW determination (Bagnaschi)

## Global fits and interpretation

prospects for the GFitter results in view of new improved experimental inputs (Schott)

## Experiments

relevance of low- and high-pile-up data (Camarda, Bendavid)

bayesian reweighing and PDF uncertainty in the  $\sin^2\theta_{\text{eff}}$  determination (Bodek)

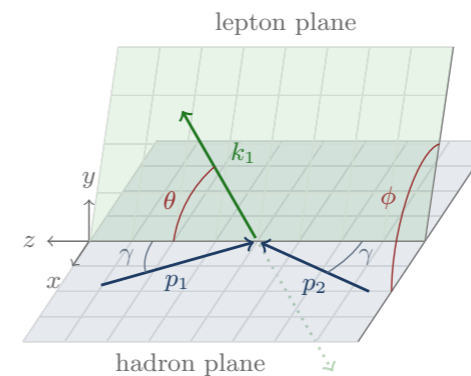
methodologies to combine the MW results of different experiments/channels/energies (Andari)

- Lepton pair production: EW precision observable

$$\frac{d^3\sigma}{dm_{ll}dy_{ll}d\cos\theta^*} = \frac{\pi\alpha^2}{3m_{ll}s} \sum_q P_q(\cos\theta^*) [f_q(x_1, Q^2)f_{\bar{q}}(x_2, Q^2) + (q \leftrightarrow \bar{q})]$$

- ATLAS 8 TeV measurement [1710.05167]

Observable	Central-Central	Central-Forward
$m_{ll}$ [GeV]	[46,66,80,91,102,116,150,200]	[66,80,91,102,116,150]
$ y_{ll} $	[0,0.2,0.4,0.6,0.8,1,1.2, 1.4,1.6,1.8,2,2.2,2.4]	[1.2,1.6,2,2.4,2.8,3.6]
$\cos\theta^*$	[-1,-0.7,-0.4,0,0.4,0.7,1]	[-1,-0.7,-0.4,0,0.4,0.7,1]
Total Bin Count:	504	150



## Triple-differential Drell-Yan cross section

- Measured with fiducial event selection cuts (on single leptons)

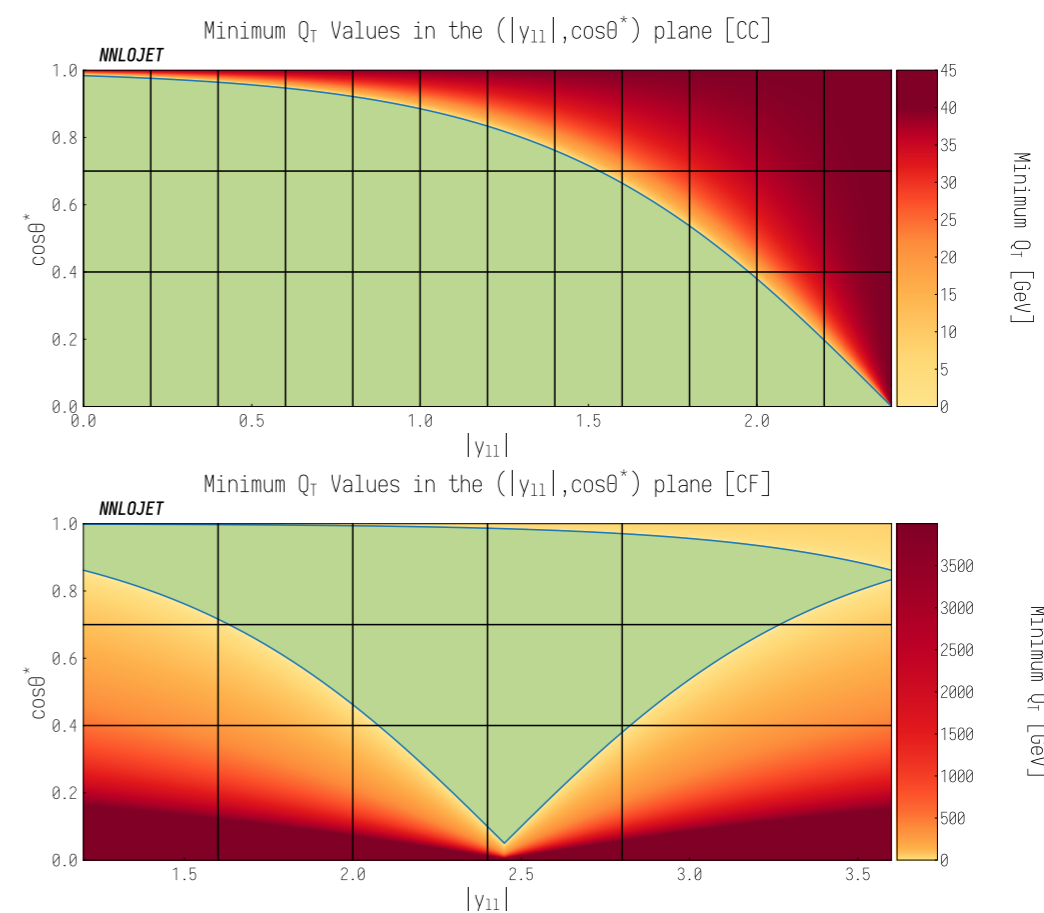
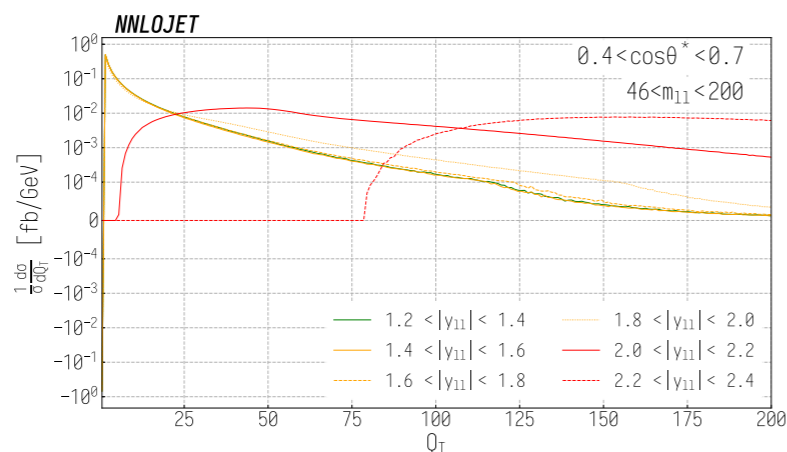
Central-Central	Central-Forward
$p_T^l > 20$ GeV	$p_{T,F}^l > 20$ GeV $p_{T,C}^l > 25$ GeV
$ y^l  < 2.4$	$2.5 <  y_F^l  < 4.9$ $ y_C^l  < 2.4$
$46$ GeV $< m_{ll} < 200$ GeV	$66$ GeV $< m_{ll} < 150$ GeV

- Fiducial cuts influence acceptances in triple-differential bins

[D.Walker, Durham 2019 PhD thesis]

# Triple-differential Drell-Yan cross section

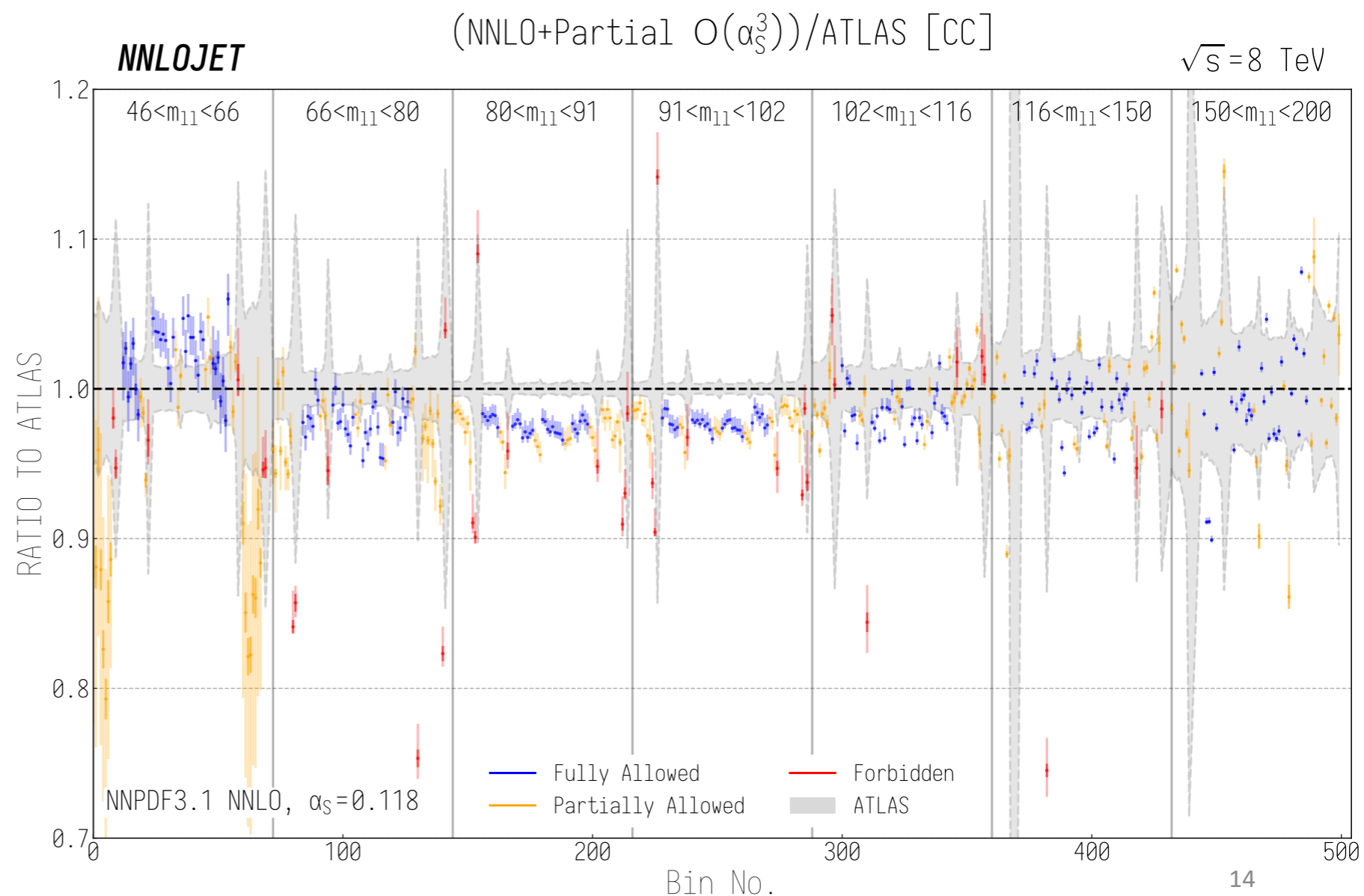
- Leading-order forbidden bins
  - require finite  $Q_T$  of lepton pair
  - shown here: symmetric lepton pair
- prediction starts only at NLO
  - lower accuracy
  - potential perturbative instabilities



# Triple-differential Drell-Yan cross section

## Including $O(\alpha_s^3)$ in forbidden bins

- improve theory uncertainty
- better agreement with data
- sizable deviations in bins around  $M_Z$
- require NLO EW



Thomas Gehrmann

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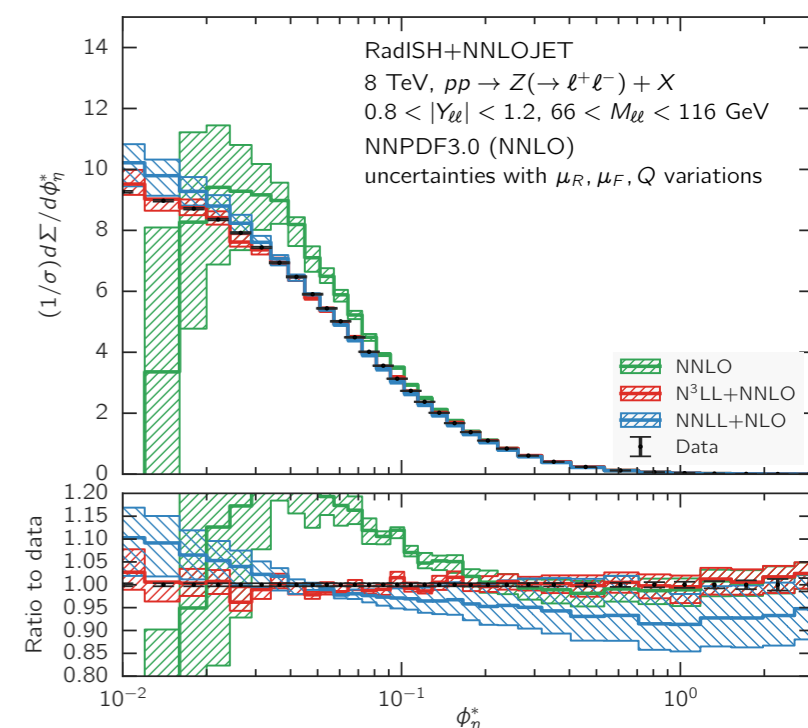
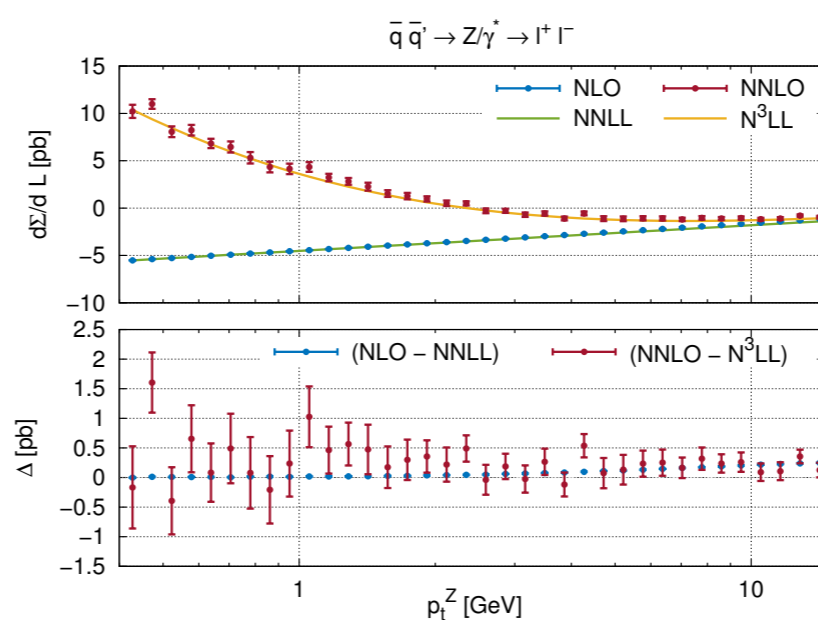
# Triple-differential Drell-Yan cross section

## Forbidden bins at leading order

- similar kinematics to  $Q_T$  or  $\phi^*$  distribution of lepton pairs
- $O(\alpha_s^3)$  corrections (Drell-Yan N<sup>3</sup>LO) obtained from V+jet at NNLO

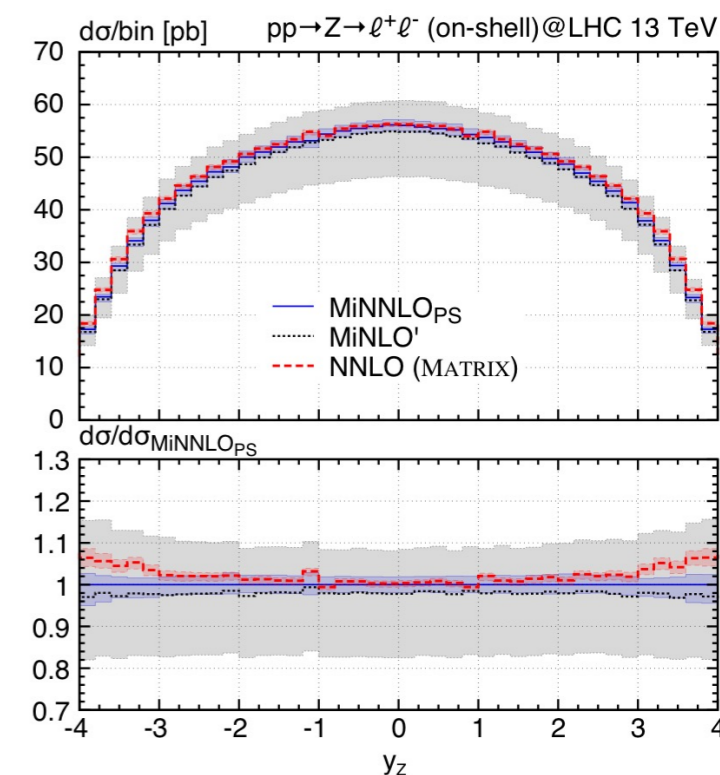
[R.Boughezal, X.Liu, F.Petriello; NNLOJET: A.Gehrmann-De Ridder, N.Glover, A.Huss, T.Morgan, D.Walker, TG]

- replace jet requirement by (small)  $Q_T$  cut
- NNLOJET: small QT region validated expanding N3LL resummation [W.Bizon, P.F.Monni, E.Re, L.Rottoli, P.Torrielli + NNLOJET]
- in future: can be matched to N3LL resummation



# Directions in precision QCD

- NNLO for higher multiplicities (beyond  $2 \rightarrow 2$ )
  - virtual two-loop amplitudes and integrals largely unknown
  - methods for handling infrared singularities becoming unpractical
  - much room for conceptual and technical progress
- Matching NNLO and parton showers
  - Higgs and Drell-Yan production [S.Höche, Y.Li, S.Prestel; P.Monni, P.Nason, E.Re, M.Wiesemann, G.Zanderighi]
- Matching NNLO and analytic resummation
  - Higgs and Drell-Yan  $q_T$  distribution [HX.Zhu et al., P.Monni et al.]
- N3LO for benchmark processes





Templates accuracy: LO		$M_W$ shifts (MeV)			
Pseudodata accuracy		$W^+ \rightarrow \mu^+ \nu$		$W^+ \rightarrow e^+ \nu$	
		$M_T$	$p_T^\ell$	$M_T$	$p_T^\ell$
1	HORACE only FSR-LL at $\mathcal{O}(\alpha)$	-94±1	-104±1	-204±1	-230±2
2	HORACE FSR-LL	-89±1	-97±1	-179±1	-195±1
3	HORACE NLO-EW with QED shower	-90±1	-94±1	-177±1	-190±2
4	HORACE FSR-LL + Pairs	-94±1	-102±1	-182±2	-199±1
5	PHOTOS FSR-LL	-92±1	-100±2	-182±1	-199±2

$pp \rightarrow W^+, \sqrt{s} = 14 \text{ TeV}$			$M_W$ shifts (MeV)			
Templates accuracy: NLO-QCD+QCD <sub>PS</sub>			$W^+ \rightarrow \mu^+ \nu$		$W^+ \rightarrow e^+ \nu(\text{dres})$	
Pseudodata accuracy		QED FSR	$M_T$	$p_T^\ell$	$M_T$	$p_T^\ell$
1	NLO-QCD+(QCD+QED) <sub>PS</sub>	PYTHIA	-95.2±0.6	-400±3	-38.0±0.6	-149±2
2	NLO-QCD+(QCD+QED) <sub>PS</sub>	PHOTOS	-88.0±0.6	-368±2	-38.4±0.6	-150±3
3	NLO-(QCD+EW)+(QCD+QED) <sub>PS</sub> two-rad	PYTHIA	-89.0±0.6	-371±3	-38.8±0.6	-157±3
4	NLO-(QCD+EW)+(QCD+QED) <sub>PS</sub> two-rad	PHOTOS	-88.6±0.6	-370±3	-39.2±0.6	-159±2

convolution with QCD can change a lot the impact of EW corrections

the bulk of the QCDxQED effects is included in the analyses  
 but  
 an estimate of the uncertainty on the size of these corrections is not available

same order as 2  $\gamma$  radiation (NNLO)



$pp \rightarrow W^+$ , $\sqrt{s} = 14$ TeV Templates accuracy: LO Pseudo-data accuracy		$M_W$ shifts (MeV)			
		$W^+ \rightarrow \mu^+ \nu$		$W^+ \rightarrow e^+ \nu$	
		$M_T$	$p_T^\ell$	$M_T$	$p_T^\ell$
1	HORACE FSR-LL	$-89 \pm 1$	$-97 \pm 1$	$-179 \pm 1$	$-195 \pm 1$
2	HORACE FSR-LL + Pairs	$-94 \pm 1$	$-102 \pm 1$	$-182 \pm 2$	$-199 \pm 1$

$\Delta M_W(\mu^+ \nu) \sim 5 \pm 1$  MeV (from  $\mu$ ) and  $\sim 3 \pm 2$  MeV (from  $e$ )

# An electroweak scheme with $(G_\mu, M_Z, \sin^2\theta_{\text{eff}})$ as inputs

M.Chiesa, F.Piccinini, AV, arXiv:1906.11569

The weak mixing angle is related to the left- and right-handed (vector and axial-vector) couplings of the Z boson to fermions

$$\sin^2 \theta_{eff}^l = \frac{I_3^l}{2Q_l} \left( 1 - \frac{g_V^l}{g_A^l} \right) = \frac{I_3^l}{Q_l} \left( \frac{-g_R^l}{g_L^l - g_R^l} \right)$$

The request that the tree-level relation holds to all orders fixes the counterterm for  $\sin^2\theta_{\text{eff}}$  on-shell definition

$$\delta \sin^2 \theta_{eff}^l = -\frac{1}{2} \frac{g_L^l g_R^l}{(g_L^l - g_R^l)^2} \text{Re} \left( \frac{\delta g_L^l}{g_L^l} - \frac{\delta g_R^l}{g_R^l} \right)$$

The renormalised angle is identified with the LEP leptonic effective weak mixing angle

The Z mass is defined in the complex mass scheme.

$\Delta r$  is evaluated with  $\sin^2\theta_{\text{eff}}$  as input and differs from the usual  $(\alpha, M_W, M_Z)$  expression

See also D.C.Kennedy, B.W.Lynn, Nucl.Phys.B322, 1; F.M.Renard, C.Verzegnassi, Phys.Rev.D52, 1369;  
A.Ferroglia, G.Ossola, A.Sirlin, Phys.Lett.B507, 147; A.Ferroglia, G.Ossola, M.Passera, A.Sirlin, Phys.Rev.D65 (2002) 113002

This scheme allows to express any observable as  $\mathcal{O} = \mathcal{O}(G_\mu, m_Z, \sin^2 \theta_{eff}^{lep})$

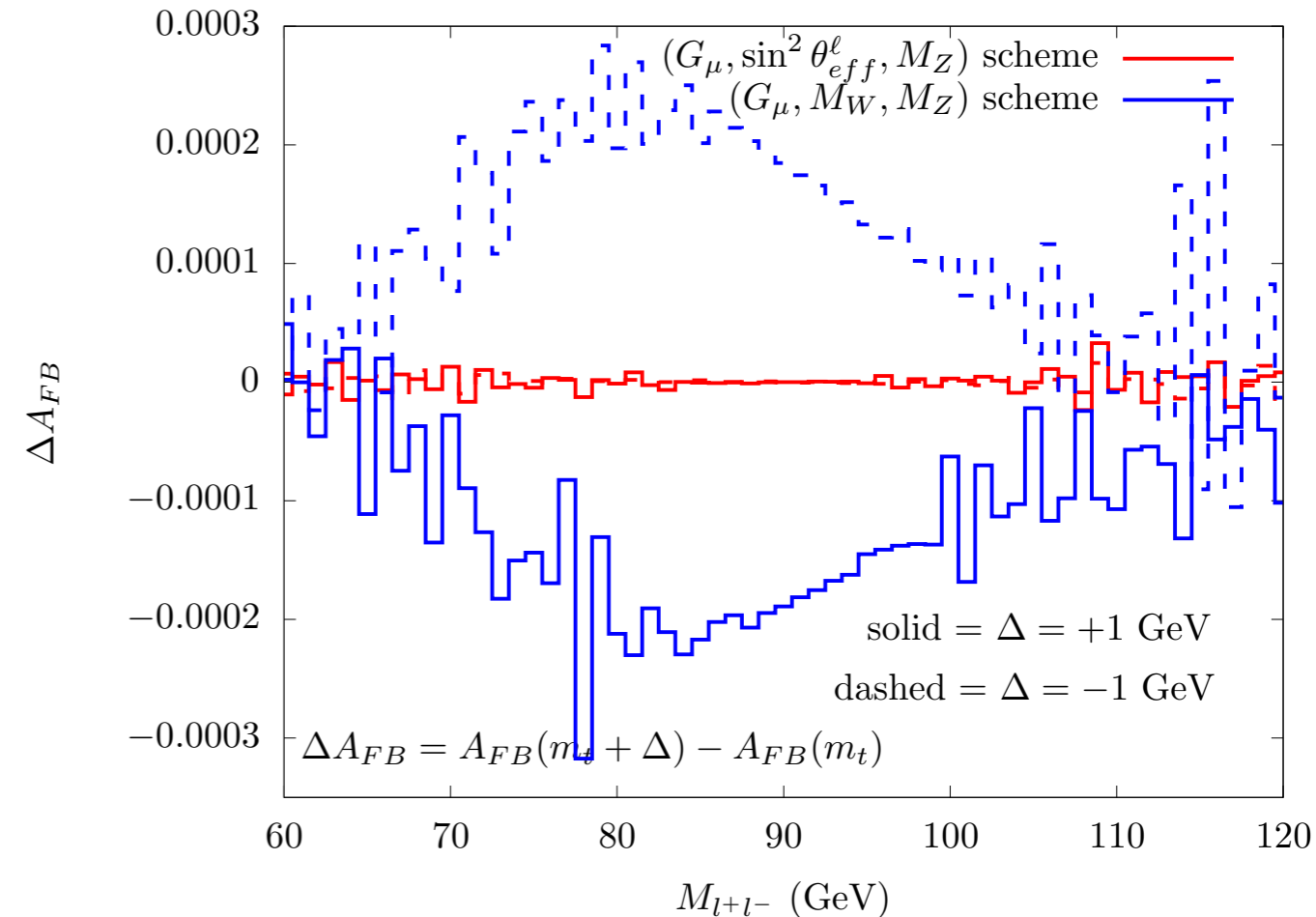
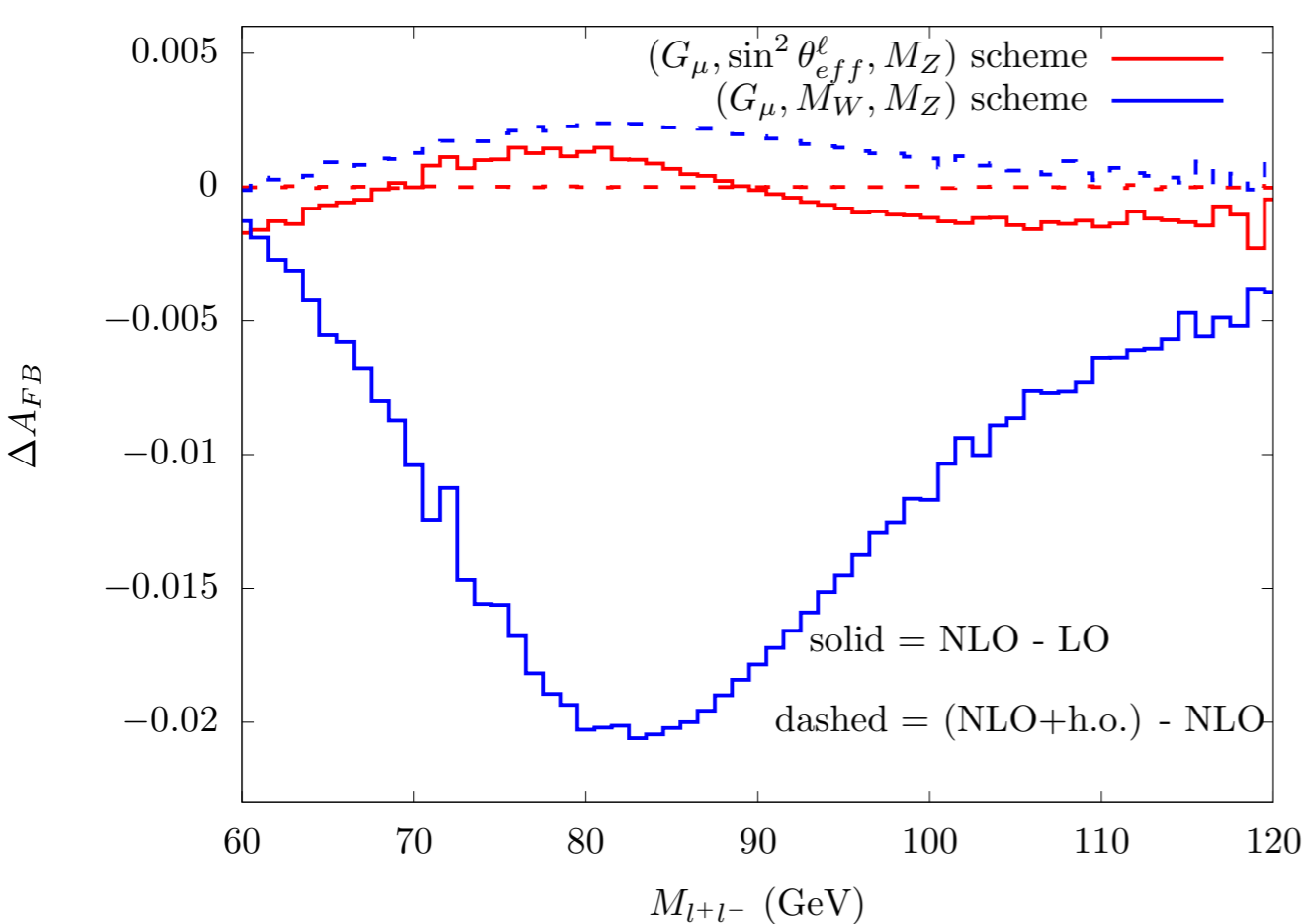
so that templates as a function of  $\sin^2\theta_{\text{eff}}$  can be easily generated

- direct relation between the data and the parameter of interest
- simple estimate of all the systematic effects, theoretical and experimental

The result of the fit in this scheme can be directly combined with LEP results

# AFB $m_{top}$ parametric uncertainties and perturbative convergence

M.Chiesa, F.Piccinini, AV, arXiv:1906.11569



prediction for AFB at the LHC in the  $(G_\mu, M_Z, \sin^2 \theta_{eff})$  input scheme (red), comparison with  $(G_\mu, M_W, M_Z)$  (blue)

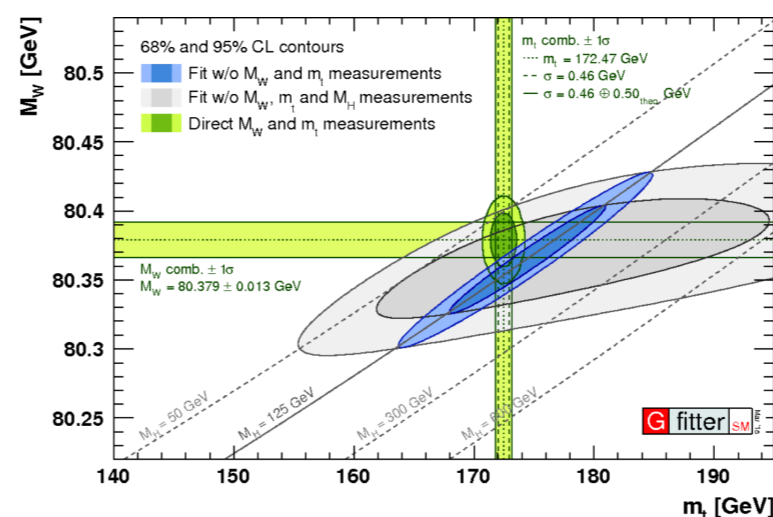
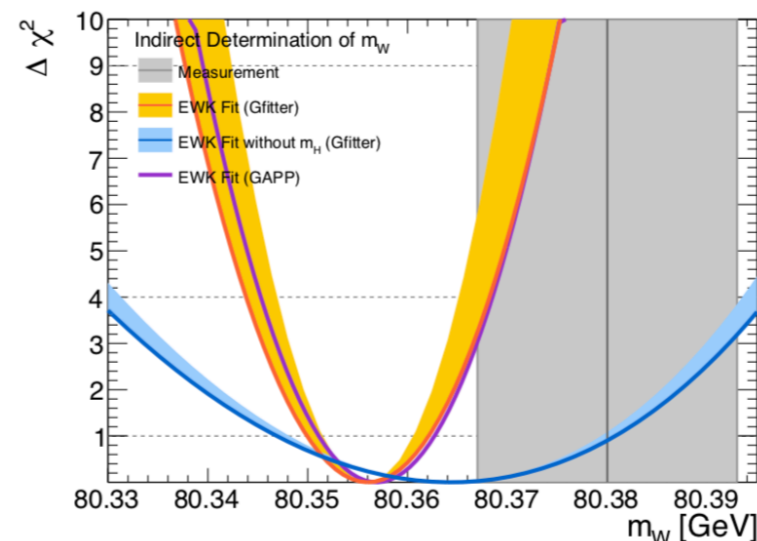
faster perturbative convergence  
 very weak parametric  $m_{top}$  dependence

→ good control over the systematic uncertainties of the templates used to fit the data

The combination  $(G_\mu, M_Z, \sin^2 \theta_{eff})$  offers a very effective parameterisation of the Z resonance in terms of normalisation, position, shape

# Interpretation in the context of the Electroweak Fit

- Unofficial combination yields a value of
  - $M_W = 80380 \pm 13$  MeV, with a p-value of 0.74
  - Several PDF correlation scenarios tested and results are stable
  
- Predicted value of the electroweak fit
  - $M_W = 80356 \pm 6$  MeV
  - $1.6\sigma$  “tension” with the SM prediction
  - Dominated by  $m_{\text{top}}$  and  $m_Z$  uncertainty, contributing 2.6 and 2.5 MeV
  - Without  $m_H$ :  $M_W = 80364 \pm 17$  MeV



The estimate of the residual theoretical error on the  $M_W$  prediction (3 MeV) is not supported by the comparison of calculations in different renormalisation schemes (OS vs  $\overline{\text{MS}}$ ) and might have a role in the significance of the fit  
 → 3-loop EW results would be needed to solve this issue

# Prospects and challenges

Two paths for future measurements at ATLAS and CMS

	High pileup	Low pileup
Most sensitive observable	$p_T$ lepton	$m_T$
Theory challenge	W/Z $p_T$ ratio, PDFs	PDFs
Experimental challenge	$p_T$ lepton calibration	Recoil calibration
Dominant uncertainties	Physics modelling, PDFs	Recoil, stat, PDFs



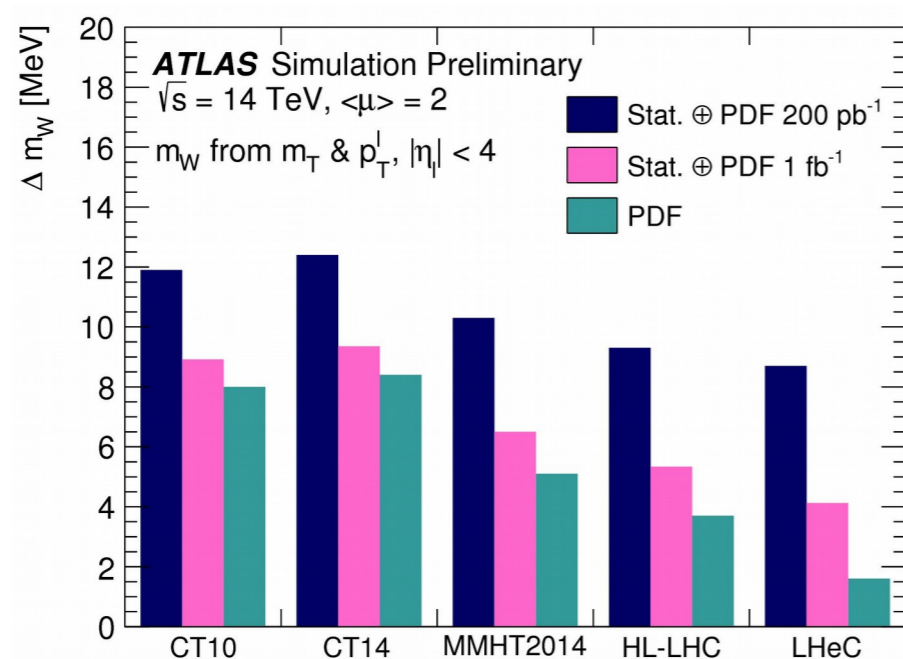
- Only option at LHCb
- Can benefit from very high stat of the HL-LHC program



- Requires dedicated runs
- Provides measurement and data-driven modelling of  $p_T$  W

- Orthogonal approaches with different dominant uncertainties
- Should be both pursued, will benefit from the combination

# Prospects for $m_W$ at the HL-LHC with low pileup data



ATL-PHYS-PUB-2018-026

- Increased acceptance provided by the new inner detector in ATLAS, (ITk) extends the coverage up to  $|\eta| < 4$
- Allows further in-situ constraints on PDFs from pseudorapidity bins
- With  $1 \text{ fb}^{-1}$  of low pileup data ( $\langle \mu \rangle \sim 2$ ) likely to reach  $\sim 6 \text{ MeV}$  of stat+PDF uncertainty
- LHeC ep collisions would largely reduce PDF uncertainties ( $< 2 \text{ MeV}$ )

## W mass at the LHC with high pileup data

- The statistical uncertainty is expected to be reduced by factors of 2 to 7 by analysing 8 and 13 TeV datasets

sqrt(s)	7 TeV	8 TeV	13 TeV
Lumi	$\sim 4.5 \text{ fb}^{-1}$	$\sim 20 \text{ fb}^{-1}$	$\sim 100 \text{ fb}^{-1}$
Events	$15 \times 10^6$	$80 \times 10^6$	$600 \times 10^6$
Stat Unc. [MeV]	7	3	1

Measured      Expected      Expected

- The muon momentum calibration uncertainty in the ATLAS 7 TeV  $m_W$  result is  $\sim 9$  MeV in the  $p_T$  lepton category and  $\sim 6$  MeV in the combined result

$ \eta_\ell $ range	[0.0, 0.8]		[0.8, 1.4]		[1.4, 2.0]		[2.0, 2.4]		Combined	
	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$
$\delta m_W$ [MeV]										
Momentum scale	8.9	9.3	14.2	15.6	27.4	29.2	111.0	115.4	8.4	8.8

- This is likely to be the dominant experimental uncertainty in high pileup measurements

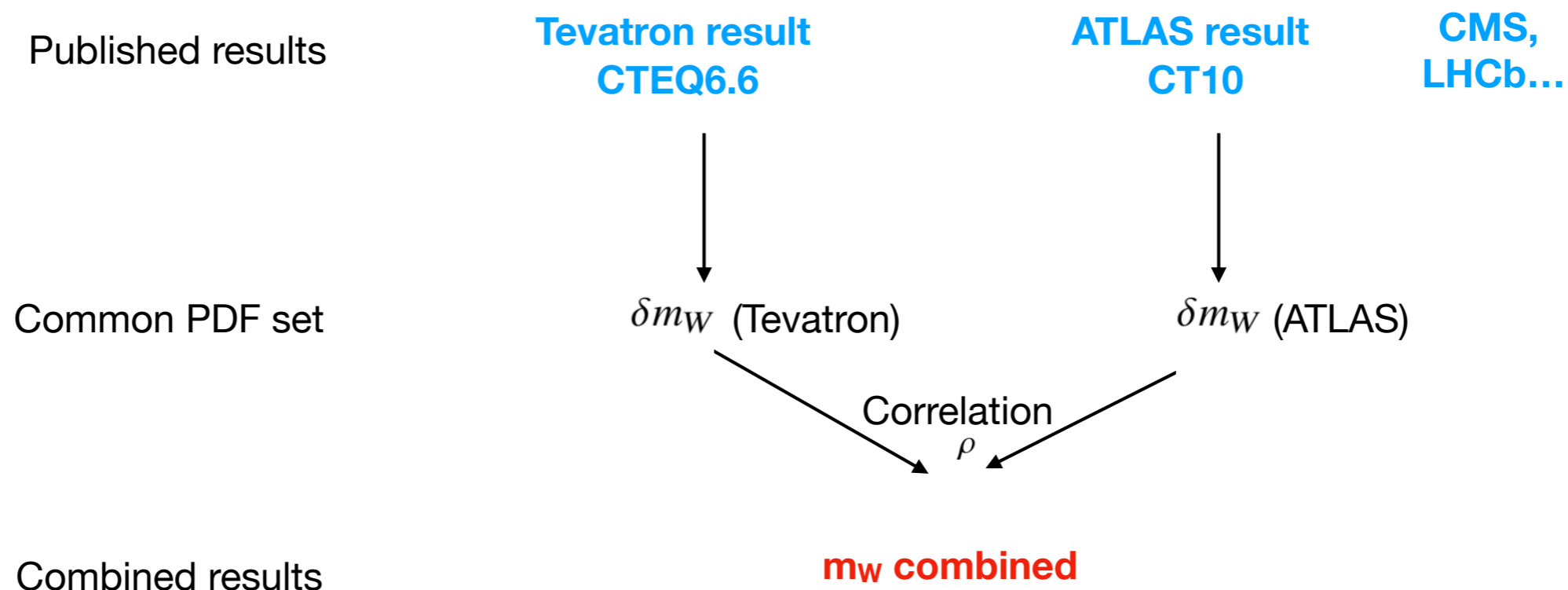


## Uncertainty correlation

	<b>ATLAS</b>	<b>Tevatron</b>
pT	Pythia8	RESBOS
A <sub>i</sub> , y	DYNNLO	RESBOS
PDF	CT10nnlo	CTEQ6.6
EW	Photos	Photos

- All experimental : uncorrelated
  - Small caveat : m<sub>Z</sub>, the primary reference for calibration in ATLAS and D0 (CDF uses J/psi)
- Physics modelling
  - Boson pT : can be assumed uncorrelated
    - Model purely based on Z data at the Tevatron
    - Combination of Z data and Z → W extrapolation at ATLAS
  - QED / EW corrections : under discussion
    - Photon radiation uncertainties
    - Radiation of pairs
    - Weak corrections
  - PDFs are the main source of correlations

**Correlation between PDF  
uncertainties to be evaluated**



- ▶ PDFs are the main source of correlations:
  - ▶ Re-create analyses on “smeared” truth-level samples (Powheg) with variety of weights corresponding to different PDFs
  - ▶ Evaluate shifts in  $m_W$  from use of different PDF sets and PDF uncertainties from EV
  - ▶ Evaluate correlations and perform combinations

## PDF uncertainties and correlations

PDF variations are applied as [event weights on the generator level](#), calculated internally in Powheg as the ratio of the event cross sections predicted by CT10 and alternative PDF sets:

- CT10 nnlo, CTEQ6.6, CTEQ6.1, MSTW2008 used in publications
- *CT10, CT14, MMHT2014, NNPDF31, CT18*: other PDF sets

Different energies 2, 7 TeV (pp-bar for 2 TeV)

$$\delta m_{W\alpha}^+ = \left[ \sum_i \left( \delta m_{W\alpha}^i \right)^2 \right]^{1/2} \quad \text{if } \delta m_{W\alpha}^i > 0, \quad \delta m_{W\alpha}^- = \left[ \sum_i \left( \delta m_{W\alpha}^i \right)^2 \right]^{1/2} \quad \text{if } \delta m_{W\alpha}^i < 0,$$

Where i runs for the uncertainty sets

$$\rho_{\alpha\beta} = \frac{\sum_i \delta m_{W\alpha}^i \delta m_{W\beta}^i}{\delta m_{W\alpha} \delta m_{W\beta}}$$

[Correlation of PDF uncertainties](#) between different categories alpha and beta

PDF correlations (preliminary; to be redone with latest inputs...)

<b>CT10</b>	1.	2.	3.	4.
1. W <sup>+</sup> 2 TeV	1	0.99	0.26	0.51
2. W <sup>-</sup> 2 TeV	0.99	1	0.31	0.52
3. W <sup>+</sup> 7 TeV	0.26	0.31	1	-0.23
4. W <sup>-</sup> 7 TeV	0.51	0.52	-0.23	1
<b>CTEQ6.6</b>	1.	2.	3.	4.
1. W <sup>+</sup> 2 TeV	1	1	0.37	0.45
2. W <sup>-</sup> 2 TeV	1	1	0.36	0.46
3. W <sup>+</sup> 7 TeV	0.37	0.36	1	-0.42
4. W <sup>-</sup> 7 TeV	0.45	0.46	-0.42	1

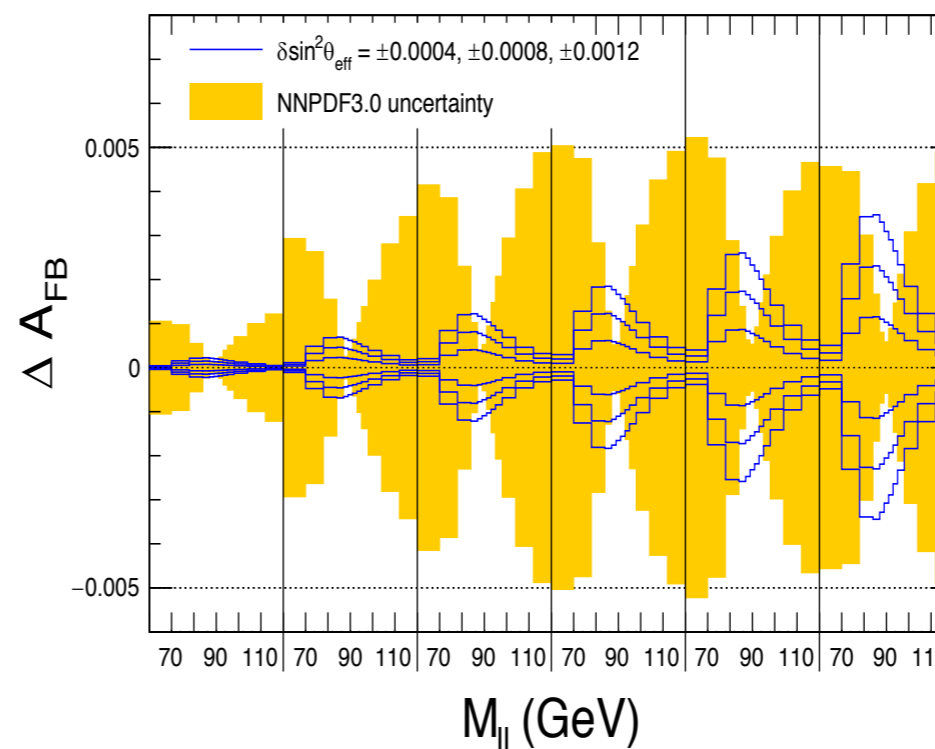
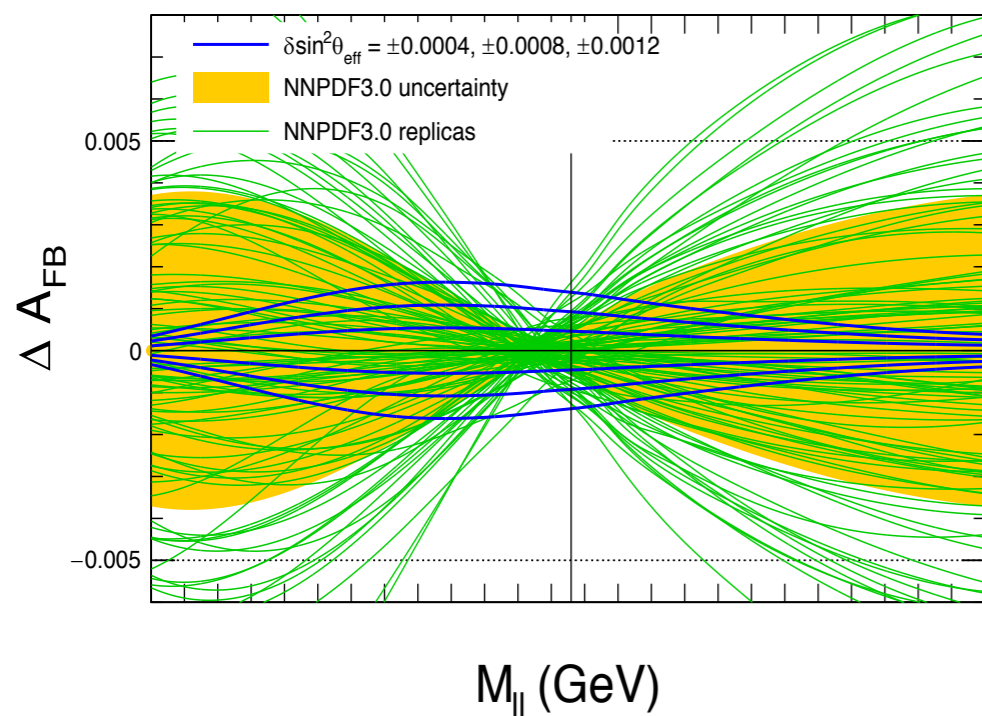
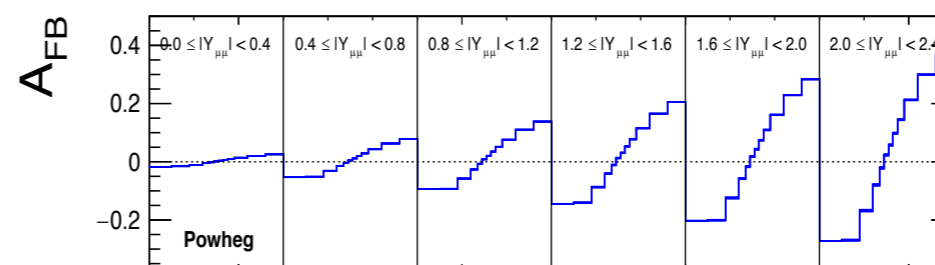
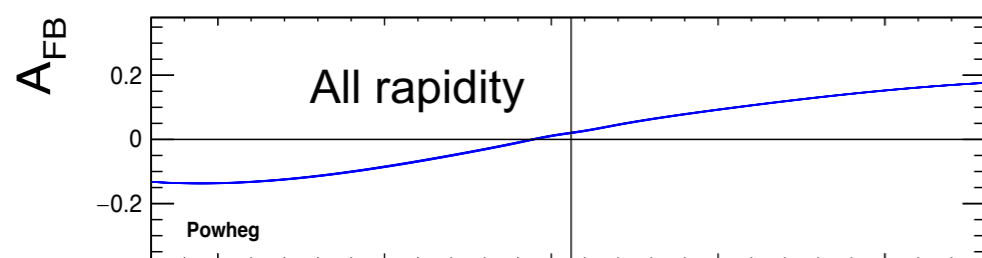
**Few % stat uncertainties to be evaluated on the correlations**

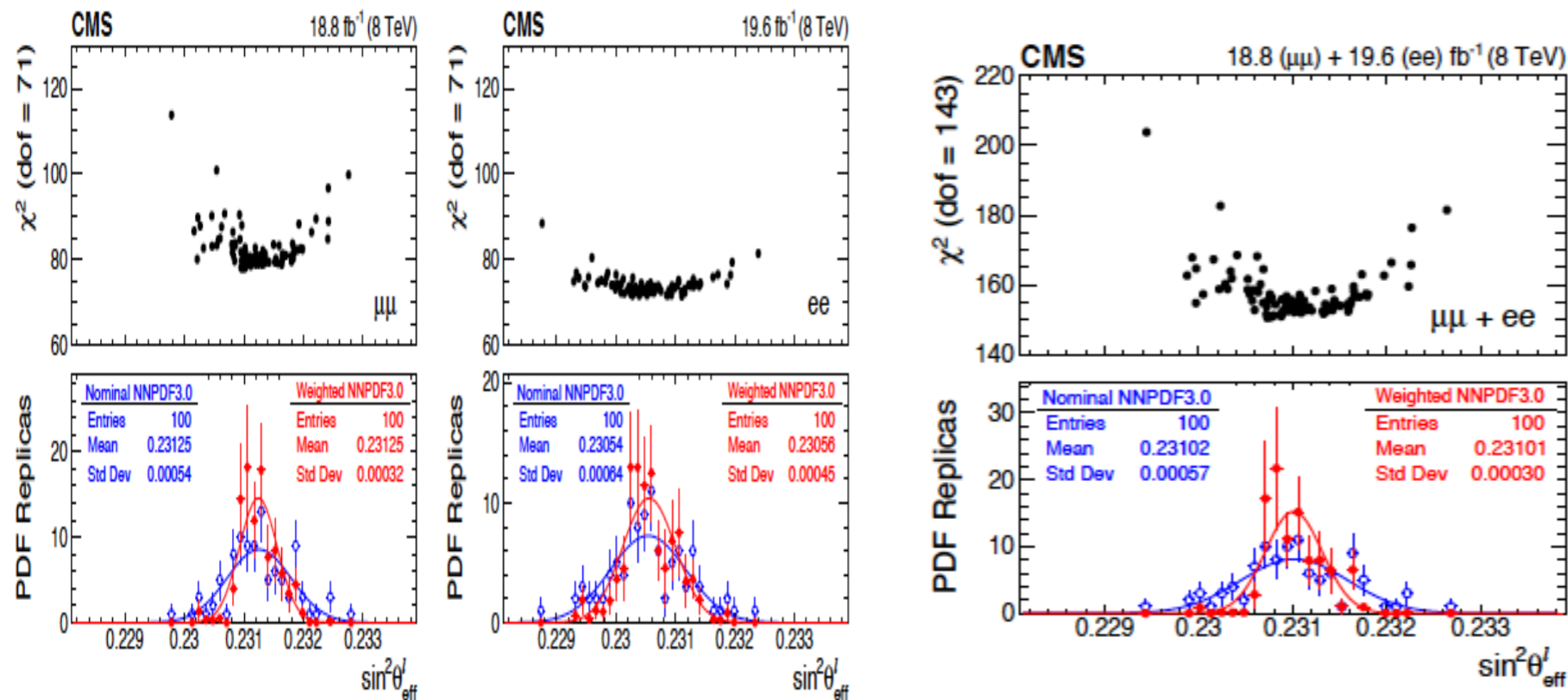
- Observed  $A_{FB}$  is very sensitive to PDFs
- Large in low and high masses, small near the peak ( + specific dependence on  $Y$  )

**CMS**



**BLUE** : Vary  $\sin^2\theta_{eff}$  for fixed PDF  
**ORANGE/green**: Vary 100 NNPDF3.0 replicas for fixed  $\sin^2\theta_{eff}$





Channel	without constraining PDF	with constraining PDFs
Muon	$0.23125 \pm 0.00048 \pm 0.00054$	$0.23125 \pm 0.00048 \pm 0.00032$
Electron	$0.23054 \pm 0.00069 \pm 0.00064$	$0.23056 \pm 0.00069 \pm 0.00054$
Combined	$0.23102 \pm 0.00040 \pm 0.00057$	$0.23101 \pm 0.00040 \pm 0.00030$

Precision Electroweak Physics

Arie Bodek, Aleko Khukhunaishvili,  
University of RochesterBayesian reweighting method  
Factor of 2 reduction in errors

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The Bayesian reweighting offers the most optimistic estimate of the uncertainty, before a new global PDF fit includes the new data

The correlation between the PDFs and  $\sin^2 \theta_{\text{eff}}$  might be better handled in a simultaneous global fit

# Conclusions

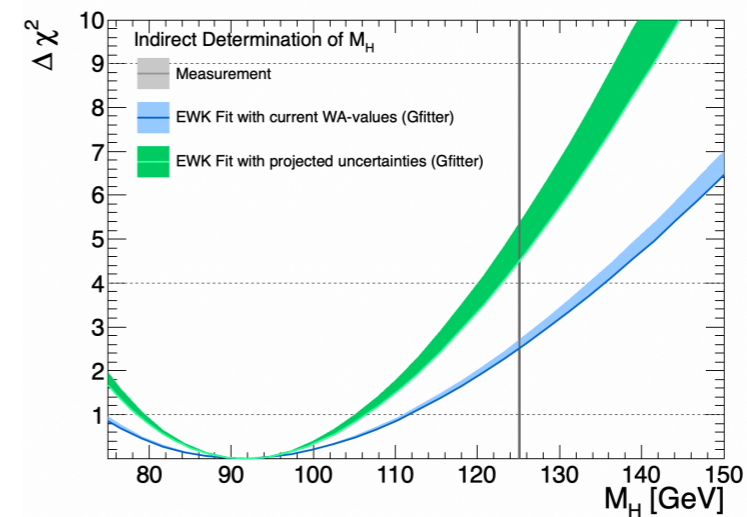
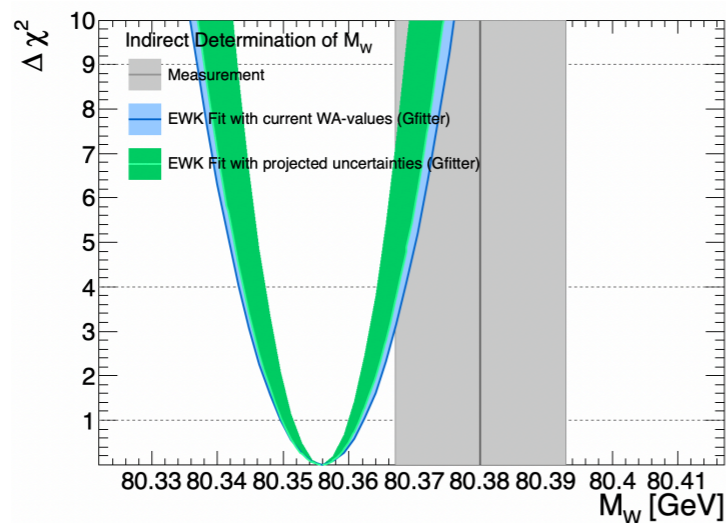
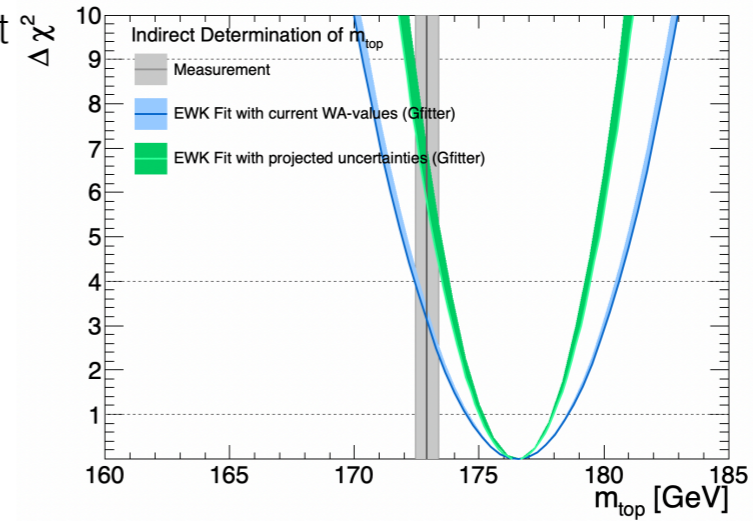
Many long and lively discussions during the Saclay workshop

More work is needed from both th and exp sides

Optimistic but challenging perspectives

# Where will we stand in 10 Years with an Ultimate Precision at the LHC?

- By the end of the LHC, we (being optimistic) might have
  - $\Delta m_W \approx 8 \text{ MeV}$
  - $\Delta m_{\text{Top}} \approx 300 \text{ MeV}$
  - $\Delta \sin^2 \Theta_W \approx 0.00012$
- ... results in indirect precisions of
  - $\Delta m_W \approx 4 \text{ MeV}$ ,  $\Delta m_{\text{Top}} \approx 1.3 \text{ GeV}$ ,  $\Delta m_H \approx 13 \text{ GeV}$
  - See also a detailed study from Gfitter from 2014: <https://arxiv.org/abs/1407.3792>



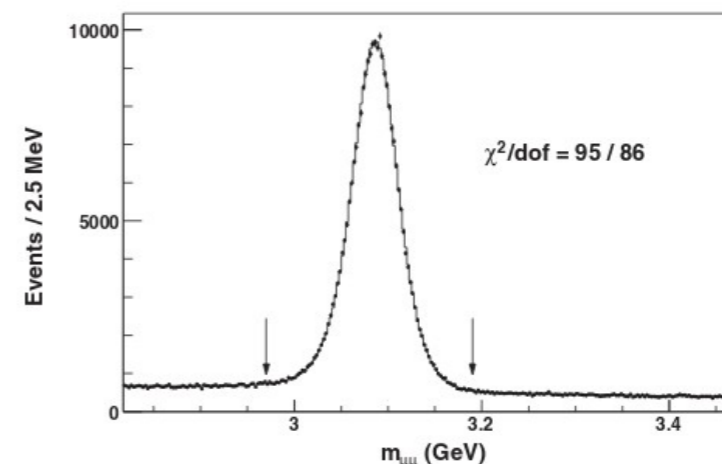
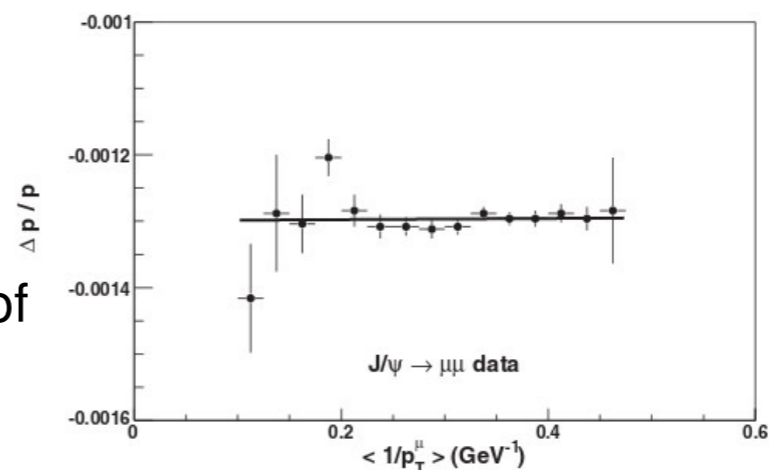


- Most measurements of  $m_W$  at hadron colliders (UA2, D0, ATLAS) lay the foundations of the energy and momentum calibration upon an external measurement of  $m_Z$
- Drawbacks:
  - Effectively provide a measurement of  $m_W/m_Z$ , and suffer from an irreducible 2 MeV uncertainty from the LEP measurement of  $m_Z$
  - Introduce correlation of momentum calibration uncertainties between different measurements

# Muon momentum calibration with $J/\psi$

- One notable exception: CDF measurement of  $m_W$  based the muon momentum calibration on  $J/\psi$  (and  $Y$ )
- Electron energy and recoil momentum are cross-calibrated to the muon-momentum scale
- Propagation of the momentum scale from  $\sim 5$  to  $\sim 80$  GeV is a great challenges, requires perfect control of
  - Misalignments
  - Magnetic field nonuniformities
  - Material and energy loss

Source	$J/\psi$ ( $\times 10^{-3}$ )	$Y$ ( $\times 10^{-3}$ )	Common ( $\times 10^{-3}$ )
QED and energy-loss model	0.080	0.045	0.045
Magnetic field nonuniformities	0.032	0.034	0.032
Ionizing material correction	0.022	0.014	0.014
Resolution model	0.020	0.005	0.005
Background model	0.011	0.005	0.005
COT alignment corrections	0.009	0.018	0.009
Trigger efficiency	0.004	0.005	0.004
Fit range	0.004	0.005	0.004
$\Delta p/p$ step size	0.002	0.003	0
World-average mass value	0.004	0.027	0
Total systematic	0.092	0.068	0.058
Statistical	0.004	0.025	0
Total	0.092	0.072	0.058



- Benefit from larger sample than  $Z$ , and more precise mass measurement ( $10^{-6}$ )